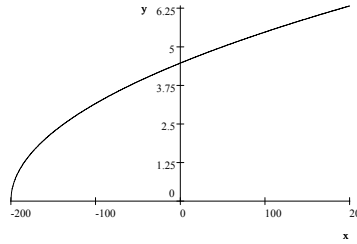


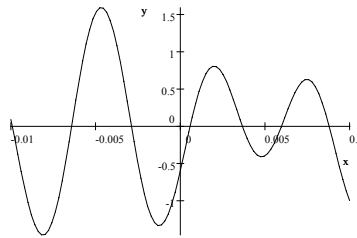
(You must show all work to get credit. Always give appropriate units.)

1. Use your calculator to get a useful view of the following functions. Sketch each curve below, label the axes, and write down the window you used (20 pts each).

- (a)  $y = \sqrt{0.1x + 20}$  (15 for reasonable plot, 10 for any reasonable window to go with plot that gives a curve like this):



- (b)  $y = \sin(1000x) - 0.6 \cos(700x)$  (15 for reasonable plot, 10 for reasonable window to go with plot; the  $x$ -window should be something like  $[-.01, .01]$ ).

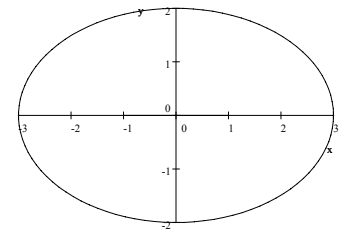
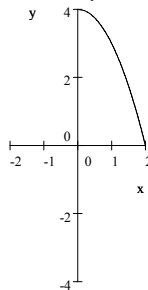
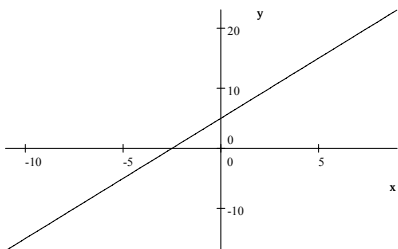


2. For each of the parametric curves below, draw a sketch on the axes provided (10pts each). Next, eliminate the parameter  $t$  to give the relation between  $y$  and  $x$  for *any two of them* (10pts each).

$$\begin{cases} x = 2t - 1 \\ y = 4t + 3 \end{cases} \quad -5 \leq t \leq 5$$

$$\begin{cases} x = \sqrt{t} \\ y = 4 - t \end{cases} \quad 0 \leq t \leq 4$$

$$\begin{cases} x = 3 \cos t \\ y = 2 \sin t \end{cases} \quad 0 \leq t \leq 2\pi$$



For the first:  $t = \frac{x+1}{2}$ , so  $y = 4\left(\frac{x+1}{2}\right) + 3 = 2x + 5$ . For the second,  $t = x^2$ , so  $y = 4 - x^2$ .

For the last,  $\frac{x}{3} = \cos t$  and  $\frac{y}{2} = \sin t$ ; thus,  $\left(\frac{x}{3}\right)^2 + \left(\frac{y}{2}\right)^2 = 1$ .

NOTE: In this last set of parametric equations, you could write  $t = \arccos(x/3)$ , so that  $y = 2\sin(\arccos(x/3))$ . However, this doesn't work completely because, by definition,  $0 \leq \arccos \theta \leq \pi$ , so  $y$  can never be negative, being the sine of an angle between 0 and  $\pi$ . Thus, we would only get the *top half* of the ellipse (try it).